

## TWO- DIMENSIONAL NUMERICAL MODEL FOR THERMAL POLLUTION OF SINGEL SOURCE IN RIVER

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### ABSTRACT

The aim of this research was to apply a numerical model capable of describing the thermal pollution in rivers. For this purpose a two-dimensional numerical model was applied for estimating temperature distribution in a river .

Momentum Conservation Equation and Thermal Energy Equation were used to describe the advection and diffusion of temperature along the river subjected to thermal pollution point source. Furthermore the model incorporates the (k-ε) turbulence model to calculate the distribution of turbulent viscosity .The pressure distribution was determined using hydrostatic pressure equation.

The partial differential equations were formalized and simplified to be solved using Alternative direction implicit- explicit method (ADI) with upwinding technique . The resulting system of linear simultaneous equations were then solved using Gauss-Elimination method .

Laboratory physical model was built to find experimental data . These data were used for model validation with data obtained from Al-Daura power station and Tigris river.

The model was found to be sensitive to the variation of river velocity and density difference and the model was found to be insensitive to the wind speed .The comparison of observed results from Al-Daura power station and laboratory physical model with those computed by the numerical model showed a good agreement . The maximum absolute difference percentage are (16.2%, 8.6%) respectively.

### الخلاصة

يهدف البحث الى بناء نموذج عددي لدراسة التلوث الحراري في الانهار الناجم عن مصدر لتلوث حراري . ولهذا الغرض تم استنباط نموذج رياضي عددي لتمثيل هذه الظاهرة والتنبؤ بتوزيع درجات الحرارة في النهر .

تم استخدام معادلة حفظ الزخم ومعادلة حفظ الطاقة ومعادلات التوزيع الحراري لمعرفة توزيع وانتشار درجات الحرارة خلال منطقة الدراسة وكذلك تضمن النموذج العددي معادلات الاضطراب لحساب معاملات اللزوجة. كما تم اعتماد معادلة الضغط الهيدروستاتيكي لحساب الضغط في كل نقطة من الدراسة .

تم تبسيط المعادلات التفاضلية المختلفة الاشكال بطريقة الاتجاه المتناوب (الضمني - الصريح) المحسنة المحددة (ADI) مع تطبيق منظومة Up Winding للحصول على معادلات جبرية خطية تم حلها بطريقة الحذف المتناوب (Gauss - Elimination) كما تم بناء نموذج مختبري لاغراض عمل التحقق لبيانات التجارب.

حي لقد وجد ان النموذج حساس الى سرعة النهر والى تغير الكثافة وان النموذج غير حساس لتغير  
ريجة الريح .

خلال مقارنة النتائج المقاسة في نهر دجلة اسفل محطة كهرياء الدورة التي تعتبر مصدر تلوث حراري للنهر  
نتج النموذج المختبري مع النتائج المحسوبة من النموذج العددي الرياضي نلاحظ انها مقبولة الى حد ما  
سنة خطأ مطلق مقدارها (16.2%، 8.6%) على التوالي.

## INTRODUCTION

The rise of water temperature due to artificial effects is called thermal pollution. This type of pollution can be defined as excessive change in the natural or ambient water temperature caused by the addition or removal of heat through man's activities. The heated water raise the temperature of the body of water above its normal level and can harm animals and plants living in the water (Richard, 2000).

The major waste-heat producing industries are :steam-electric generation plants , petroleum refineries , steel mill , chemical plants (mathur, 1976).

The discharge of heated water directly to the river can be more dangerous to the health of the receiving water than organic pollution. Higher temperature reduces solubility of oxygen. Moreover, the chemical reactions will proceed to a faster pace, hence , the water may go anaerobic with disastrous effects on its odor and appearance (Rute and Siliva, 1997).

Al-Challabi (1994) developed a two- dimensional numerical model for the simulation of the spread and mixing of thermally polluted water disposed into the flow. This model considers the effect of density difference between the pollutant density and the river water density

Li-Renyu and Righetto (1998) presented unsteady state two dimensional model to simulate the velocity and temperature field in the estuary of the Yangtza River in Brazil. It was found that the simulation by using (K-ε) model can provide more details of flow fields and temperature distribution than that once obtained by using

Phenomenological algebraic for models of eddy viscosity and diffusivity Catirolgu and Yuruk (1998) presented a mathematical model to predicts the long-term effects of once-through systems on local fish population. . The simulation indicates that entertainment and impingement may lead to a population reduction of about 2% to 8% in the long run. Joody (2001) developed one and two dimensions numerical model for the simulation of the spread and mixing of thermally polluted water disposed into the river flow released from the AL-Daura Power Station starting from the outfall up to 1000m downstream. The two dimensional model also discusses two cases, the first case neglects the effect of vertical velocity distribution while the second case includes it. Comparison of observed data on Feb 3, 2001 and July 27, 2001 with data computed by the two dimensional model shows a good agreement with percentage error of 0.57% and 1.95% respectively. In this research the finite difference method was used to solve the equations governing the phenomena of heat disposal. The solution was verified by a laboratory experimental work and field data obtained from Al-Daura power station .

## NUMERICAL MODELING

Numerical model of thermal pollution is used by the formulation of the following set of partial differential equations: (Rastogi and Rodi, 1978)

**Momentum Conservation Equations**

Horizontal Momentum Equation :

$$\frac{\partial U}{\partial t} + U \frac{\partial U}{\partial X} + W \frac{\partial U}{\partial Z} = \frac{\partial}{\partial X} \left( \mu \frac{\partial U}{\partial X} \right) + \frac{\partial}{\partial Z} \left( \mu \frac{\partial U}{\partial Z} \right) \quad (1)$$

Vertical Momentum Equation :

$$\frac{\partial W}{\partial t} + U \frac{\partial W}{\partial X} + W \frac{\partial W}{\partial Z} = \frac{\partial}{\partial X} \left( \mu \frac{\partial W}{\partial X} \right) + \frac{\partial}{\partial Z} \left( \mu \frac{\partial W}{\partial Z} \right) - \frac{\partial P}{\partial Z} + \rho g \quad (2)$$

Thermal Energy Equations :

$$\frac{\partial T}{\partial t} + U \frac{\partial T}{\partial X} + W \frac{\partial T}{\partial Z} = \frac{\partial}{\partial X} \left( \frac{\mu}{\sigma} \frac{\partial T}{\partial X} \right) + \frac{\partial}{\partial Z} \left( \frac{\mu}{\sigma} \frac{\partial T}{\partial Z} \right) + \frac{\alpha(T - T_r)}{C_p * H} \quad (3)$$

K-ε turbulence model :

K Equation :

$$\frac{\partial K}{\partial t} + U \frac{\partial K}{\partial X} + W \frac{\partial K}{\partial Z} = \frac{\partial}{\partial X} \left( \mu \frac{\partial K}{\partial X} \right) + \frac{\partial}{\partial Z} \left( \mu \frac{\partial K}{\partial Z} \right) + G - \rho \epsilon \quad (4)$$

ε Equation :

$$\frac{\partial \epsilon}{\partial t} + U \frac{\partial \epsilon}{\partial X} + W \frac{\partial \epsilon}{\partial Z} = \frac{\partial}{\partial X} \left( \mu \frac{\partial \epsilon}{\partial X} \right) + \frac{\partial}{\partial Z} \left( \mu \frac{\partial \epsilon}{\partial Z} \right) + C_1 \frac{\epsilon}{K} G - C_2 \rho \frac{\epsilon}{K} \quad (5)$$

Density- Temperature relation ships.

$$\rho = 999.8425 - 0.0055T^2 + 0.0182 T + 1000.1 \quad (6)$$

Longitudinal velocity vertical distribution:

$$U = 2.5 U_r \ln(Y/Y_0) \quad (7)$$

Pressure distribution along the river depth

$$P = \int_0^z \rho g dz \quad (8)$$

finite difference was used for the solution of the above partial differential equations, and by using the assumption to transform these equation from non-linear to linear equations (Smith, 1978). These equations are simplified in a two-dimensional vertical and horizontal direction . computer programming was used to perform the computations of the simulation model . It was written in Fortran-77 which works with Visual Fortran -97 language:

Equations (1,2,3) are considered as the three\_ dimensional governing differential equations while equations (4,5,6,7)are the auxiliary equations .

**EXPERIMENTAL WORK**

Laboratory; physical model as shown in Fig. (1) was built to simulate the case of thermal pollution in rivers in order to obtain data for verification of the numerical model mentioned above. This model was built using galvanized steel pipes and tanks. Two pumps were used one for the heated water and one for the water that simulate the river water. The water was heated using electrical heater .The water pipe was connected to the ground tank (feed tank),which then lifted to tanks number 1, and 2. The water in those tanks were connected to a glass flume which simulate the river through pipes ended by a tap after passing through electrical heaters (plant 1, and plant 2). The flume was fed by water from a re-circulation tank (tank no. 3). The flow was controlled by a weir

located at the end of the flume. The experiments was conducted to find the temperature along the flume downstream of the heated water outfall(the water from the tap). The temperature values were measured using thermometers distributed at selected distances from this tap.

Field data obtained from Al-Daura power station were also used to support this verification. **Table(1)** shows the comparison of the temperature values along the Tigris river downstream of Al doura Power station outfall with those obtained by the numerical model .The required information about Tigris river obtained from (Euphrates center for studying and design or irrigation project, 2001)

Table (1) Observed and Predicted temperature from Al-Daura power station

Distance(m)	Observed Temp.° C	Predicted Temp. °C(by Numerical model)	Absolute difference %
Outfall	44	44	0
50	32.7	38	16.2
100	30.8	34.5	12
150	30.5	32	5
200	30.3	30.6	0.004
250	30	30	0
300	29.8	29.8	0
350	29.7	29.7	0
400	29.7	29.7	0
450	29.7	29.7	0
500	29.7	29.7	0

**Table(2)** shows the comparison of the temperature values observed from the laboratory model downstream of the point source outfall with those obtained by the numerical model .

Table (2) Observed and Predicted Temperature Data from Laboratory Physical Model.

Distance (m)	Observed temp.° C (in the laboratory model)	Predicted temp.° C(by the numerical model)	Absolute Differ %
0	55	55	0
0.5	38	41.3	8.6
1	32	33.1	3.4
1.5	30	30.6	2
2	30	30.1	0
2.5	30	30	0
3	30	30	0
3.5	30	30	0
4	30	30	0

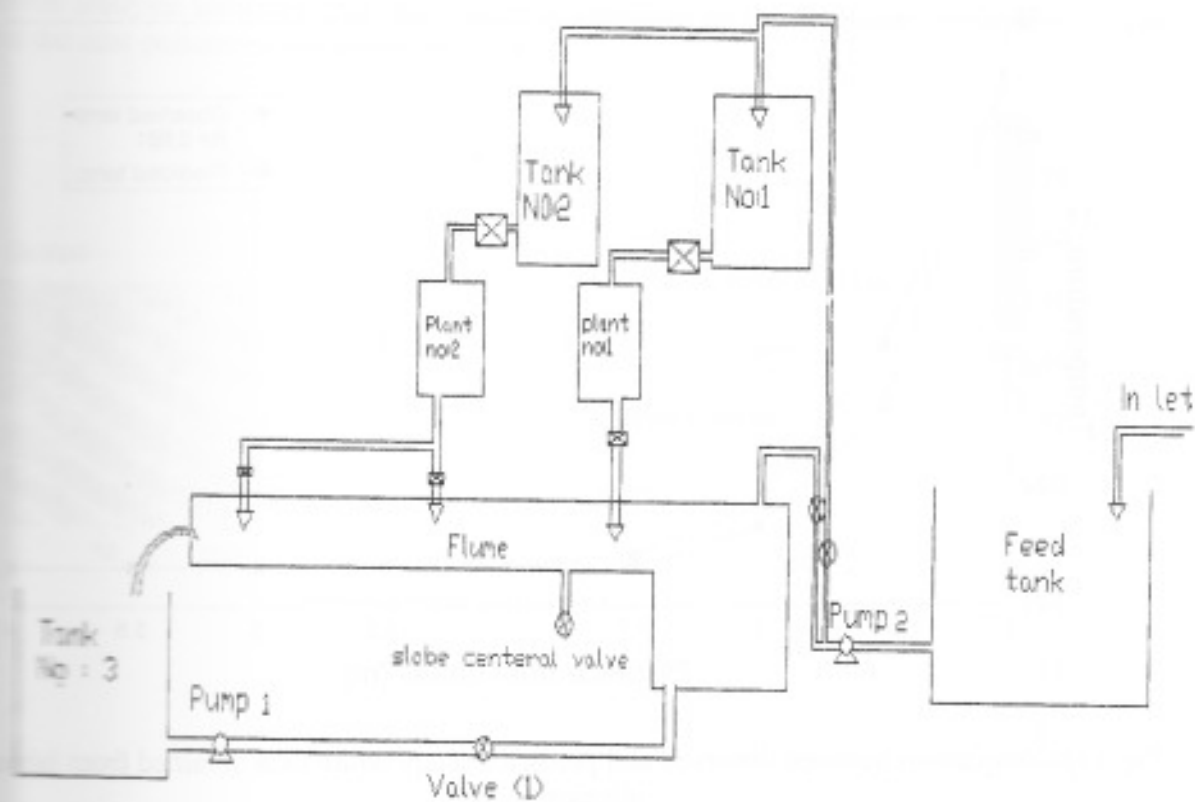


Fig. (1) Physical laboratory model

## RESULTS AND DISCUSSION

Using the results of the numerical model to study the effect of different parameters on the temperature distribution the model should be verified. The verification was carried out by conducting a comparison between the observed results from laboratory physical model and Al-Daura power station with predicted results obtained from numerical model as shown in Figs. (2,3). The maximum percentage difference was found to be (16.2%, 8.6%), and the correlation coefficient between those results are (0.917, 0.991) respectively.

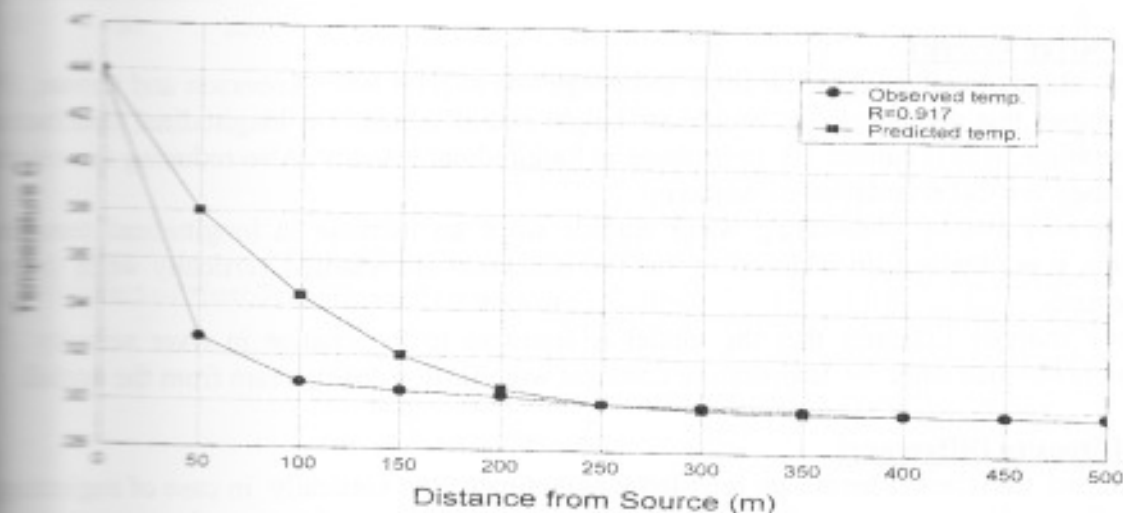


Fig. (2) Comparison between observed and predicted temperature data obtained from Al-Daura power station.

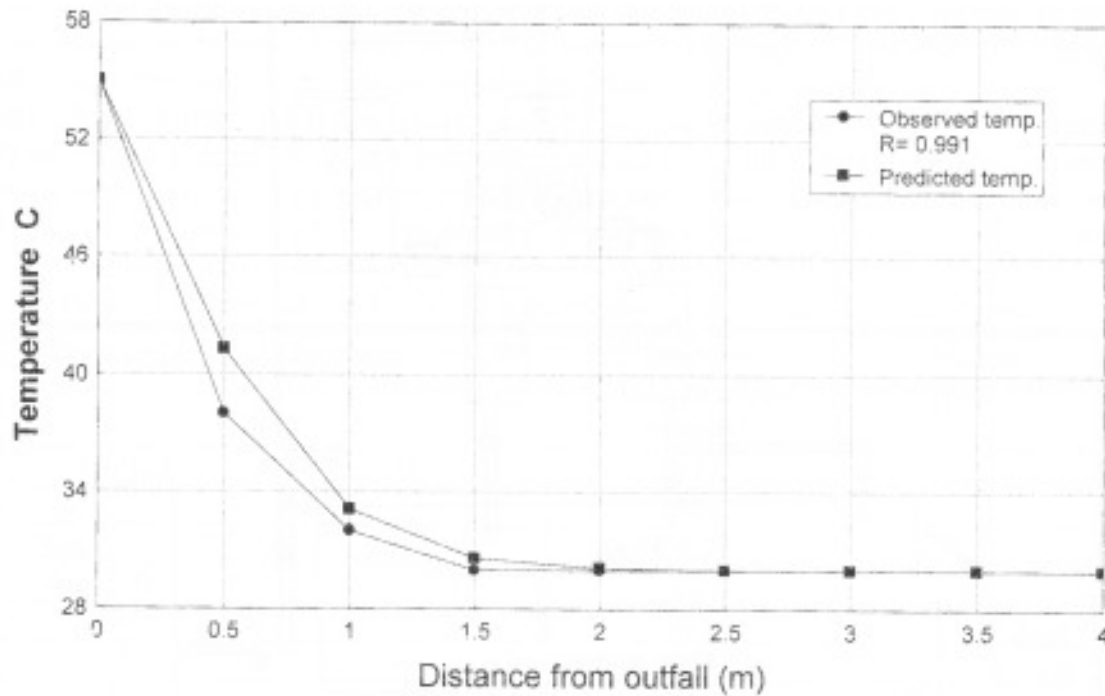


Fig. (3) Comparison between observed and predicted temperature data obtained from laboratory physical model.

### SENSITIVITY ANALYSIS

Sensitivity analysis was carried out to obtain the effect of the several important model parameters on the temperature distribution as follows:

#### Effect of Wind Speed

Fig. (4) shows the comparison between the results obtained by excluding and including heat transfer coefficient respectively. From this figure, it can be found that excluding or including heat transfer from the water surface showed no noticeable change in temperature distribution. The above analysis indicated that the model is insensitive to the variation in the wind speed. This is obvious from the comparison of the temperature contours for the two cases which is almost similar.

#### Effect of River Velocity

The river velocity is effected by the slope and roughness of river bed. (Roberson and Crowe, 1997) Fig. (5) shows that decreasing the roughness height causes increase in longitudinal distribution of the temperature. This is caused due to increase in longitudinal velocity. Also reducing the roughness height causes vertical retardation of isotherms.

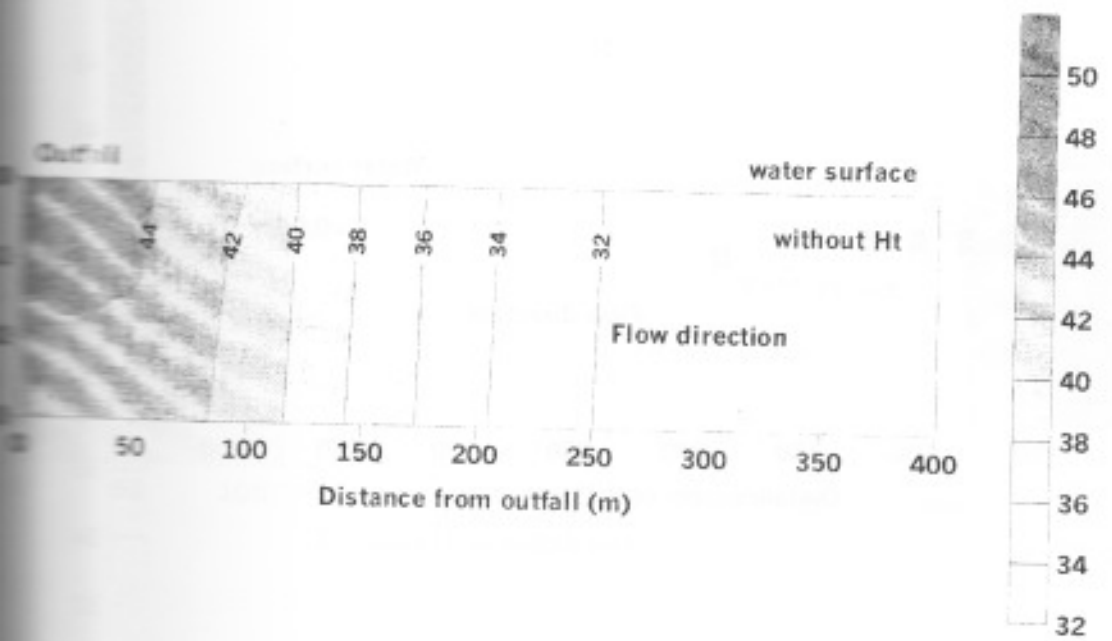
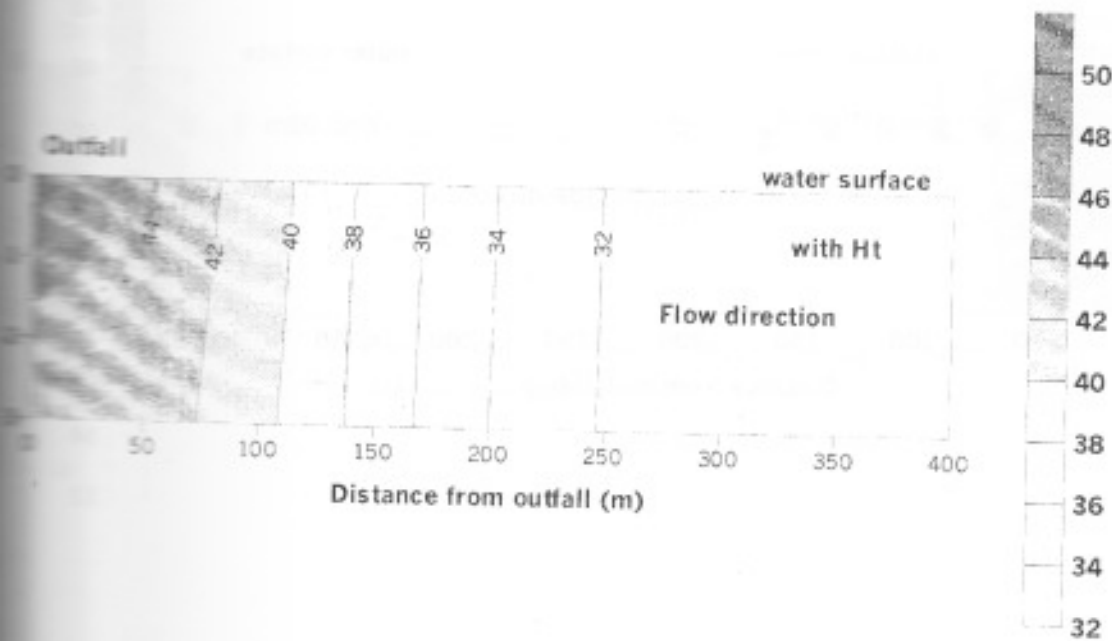
Fig. (6) shows that by increasing water surface slope an increase in longitudinal temperature distribution was obtained, in addition to this the isotherms are retarded vertically when the water surface slope increase.

The above analysis indicates that the model is sensitive to the change in river velocity. This indication is obvious since the temperature contours were shifted downstream from the outfall.

#### Effect of Density Difference:

Fig. (7) shows that the isotherms are retarded longitudinally and vertically in case of neglecting density effect. This can be attributed to the effect of a buoyancy force on the spreading of temperature.

The above analysis indicates that the model is sensitive to the variation of density difference between the heat polluted water and river water.



Effect of Heat Transfer on Temperature Distribution. ( $T_d=50\text{ }^\circ\text{C}$ ,  $T_r=30\text{ }^\circ\text{C}$ ,  $t=300\text{sec}$ )

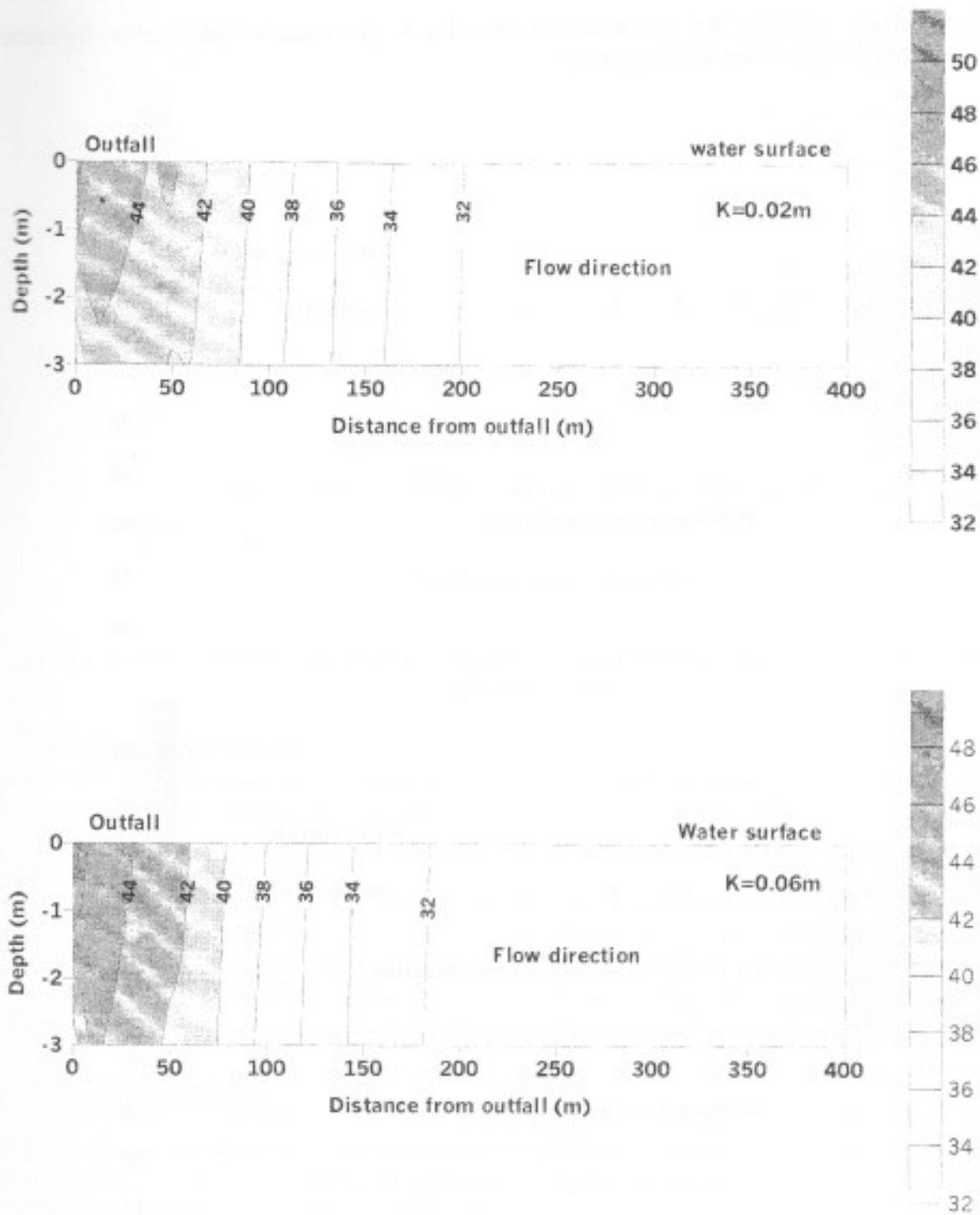
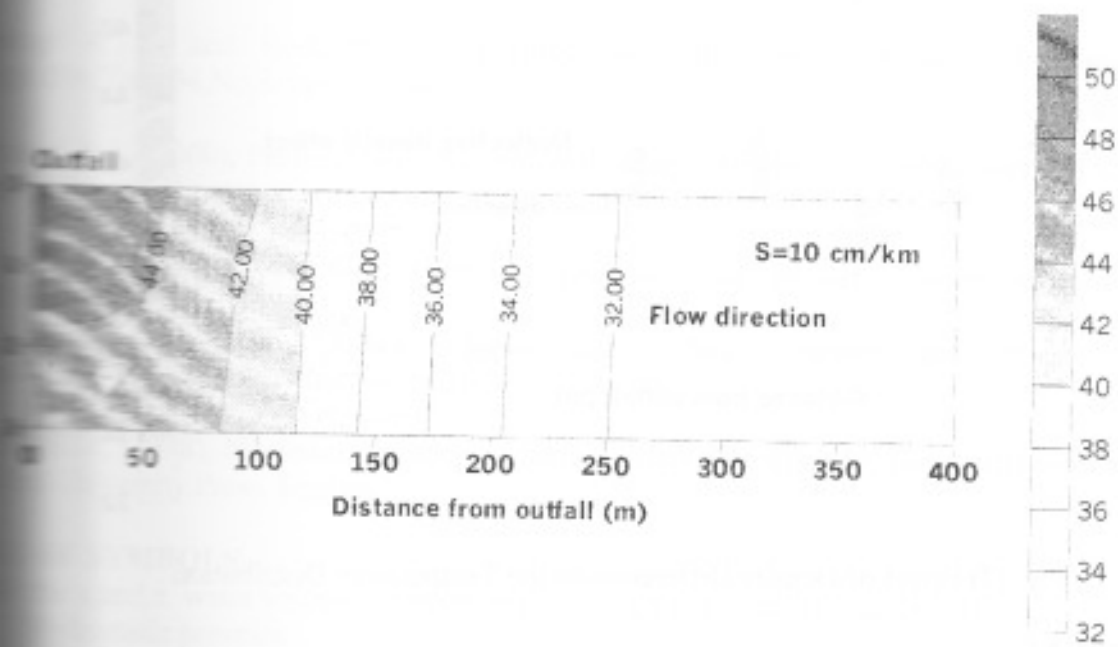
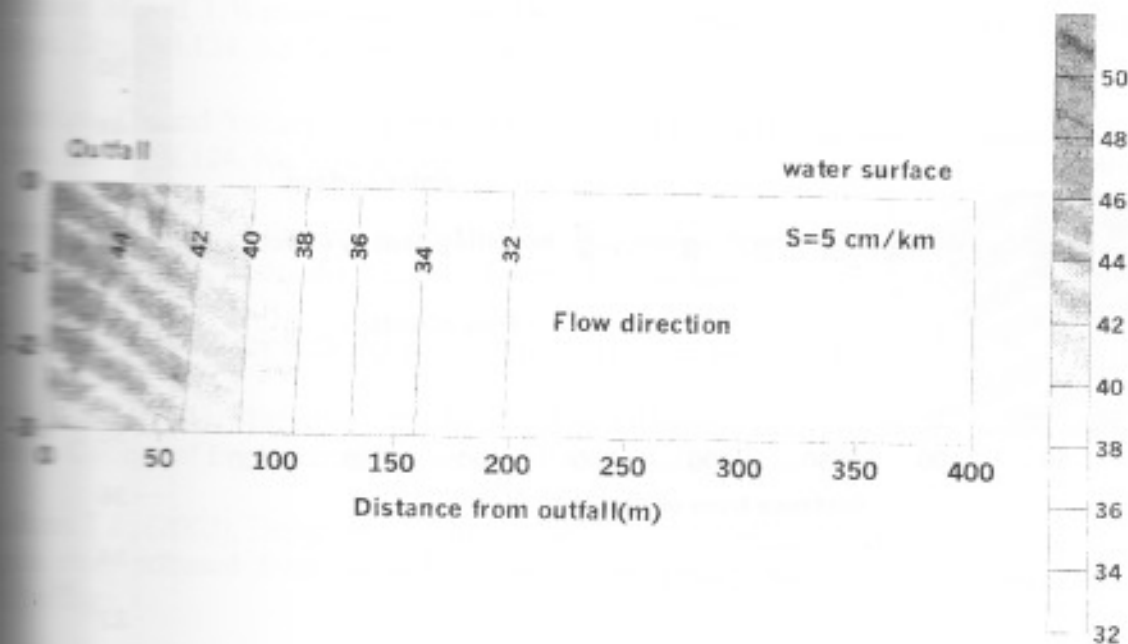


Fig. (5) Effect of Roughness Height on Temperature Distribution . ( $T_r=30\text{ }^\circ\text{C}$ ,  $T_d=50\text{ }^\circ\text{C}$ ,  $t=300\text{sec}$ )





6) Effect of River Slope on Temperature Distribution .(  $T_r=30 \text{ }^\circ\text{C}$ ,  $T_d=50 \text{ }^\circ\text{C}$ ,  $t=300\text{sec}$ )

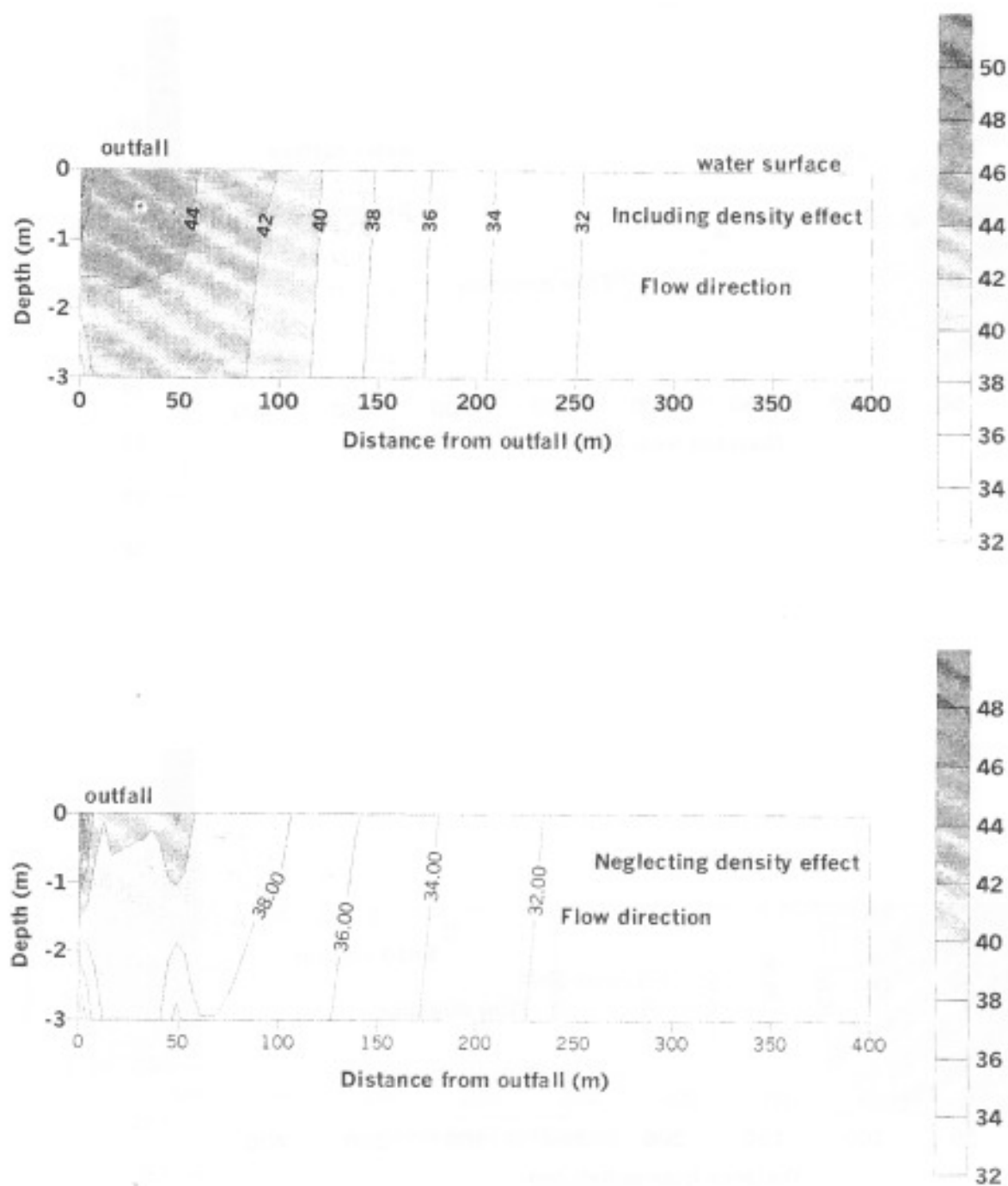


Fig. (7) Effect of Density Difference on the Temperature Distribution .

## CONCLUSIONS

- 1- The numerical model is insensitive to the variations of wind speed .
- 2- The numerical model is sensitive to the variation of roughness height of the river bed , slope of water surface , density difference between the heated water density and the river water density .
- 3- The model can be utilized to study the effect of various physical parameters on temperature distribution .

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#### LIST OF SYMBOLS

- $u, v, \text{ and } w$  water velocity components in x, and, z components respectively
- $p$  Hydrostatic pressure
- $g$  Gravitational acceleration
- $U_0$  Surface wind velocity at distance  $y_0$  from ground
- $U_y$  Wind velocity at any depth  $y$  from ground surface
- $T_w$  Water temperature
- $H$  River Roughness Height
- $\rho_w$  Water Density
- $T_{ws}$  Source Water Temperature
- $T_w$  River Water Temperature